

# Multiphoton Microwave Ionization of Rydberg Atoms

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## Rydberg Atoms and How They Ionize

Introduction to Rydberg Atoms

Field Ionization

Photoionization

MW Ionization

## Experimental Setup

Experimental Apparatus

## Experimental Results

Multiphoton MW Ionization

Single Photon Ionization Rates

Above-Threshold Bound States

# Acknowledgments

Professor Tom Gallagher

Dr. Haruka Maeda

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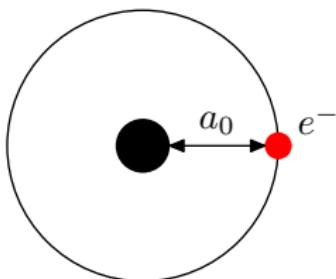
Dr. Wei Yang

Dr. Jianing Han

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Paul Tanner

# Atomic Units



Mass	$m_e$	$9.1 \times 10^{-31}$ kg	= 1
Action	$\hbar$	$1.05 \times 10^{-34}$ J·sec	= 1
Charge	$e$	$1.6 \times 10^{-19}$ C	= 1
Length	$a_0$	$5.29 \times 10^{-11}$ m	= 1
Energy	W	$2 \times 13.6$ eV	= 1
Frequency	$\omega/2\pi$	$6.5761 \times 10^6$ GHz	= 1
Electric Field	E	$5.137 \times 10^9$ V/cm	= 1

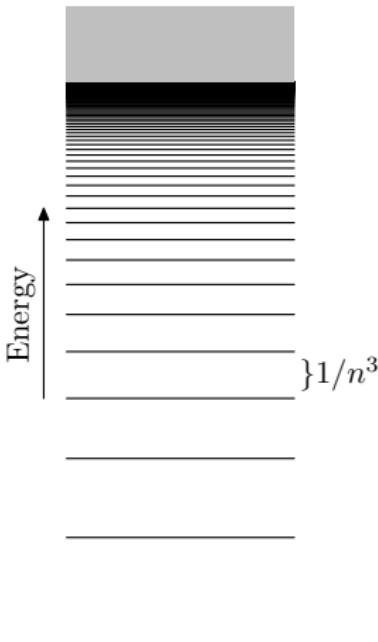
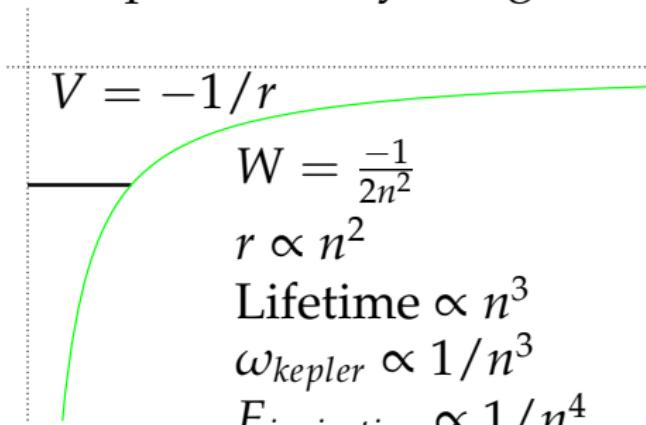
# What's a Rydberg Atom?

Any atom with one or more electrons of large principal quantum number  $n$ , where  $n > 10$ .

This Talk:  $70 < n < 600$

# Introduction to Rydberg Atoms

## Properties of Rydberg Atoms



# Introduction to Rydberg Atoms

## Properties of Rydberg Atoms

$$V = -1/r$$

$$W = \frac{-1}{2n^2}$$

$$r \propto n^2$$

$$\text{Lifetime} \propto n^3$$

$$\omega_{\text{kepler}} \propto 1/n^3$$

$$E_{\text{ionization}} \propto 1/n^4$$

For  $n=100$ :

- ▶  $W = -1.4 \text{ meV}$
- ▶  $\langle r \rangle = 0.5 \mu\text{m}$
- ▶  $\tau = 1 \text{ ms}$
- ▶  $\omega_{\text{kepler}} = 2\pi \times 6.5 \text{ GHz}$
- ▶  $E_{\text{ionization}} = 5.7 \text{ V/cm}$

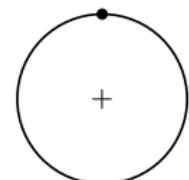
# Non-hydrogenic Atoms

$$\begin{array}{c} n \\ \hline - - - - - \\ np \qquad nd \qquad nf \end{array}$$

Ion core  
interactions shift  
energy levels

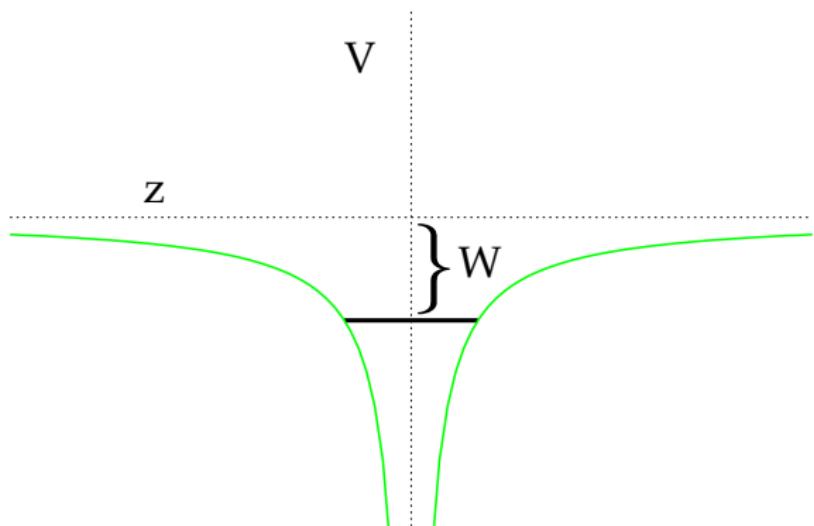
$$\begin{array}{c} \\ \hline ns \end{array}$$

$$W = \frac{-1}{2(n - \delta_\ell)^2}$$



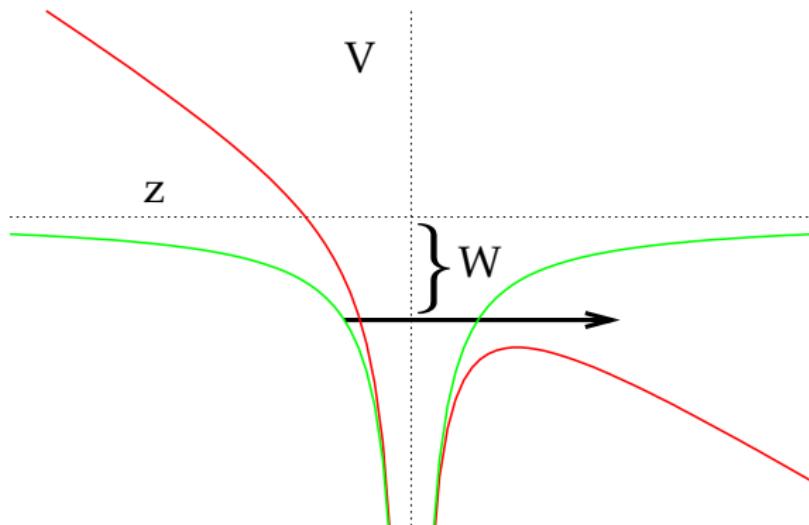
$$\begin{array}{c} n - 1 \\ \hline - - - - - \end{array}$$

# Field Ionization



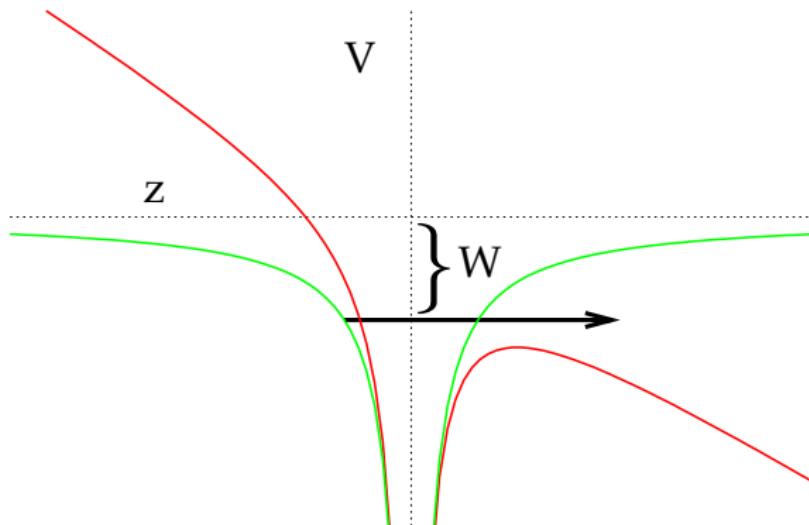
$$V(z) = \frac{-1}{|z|}$$

# Field Ionization



$$V(z) = \frac{-1}{|z|} - Ez$$

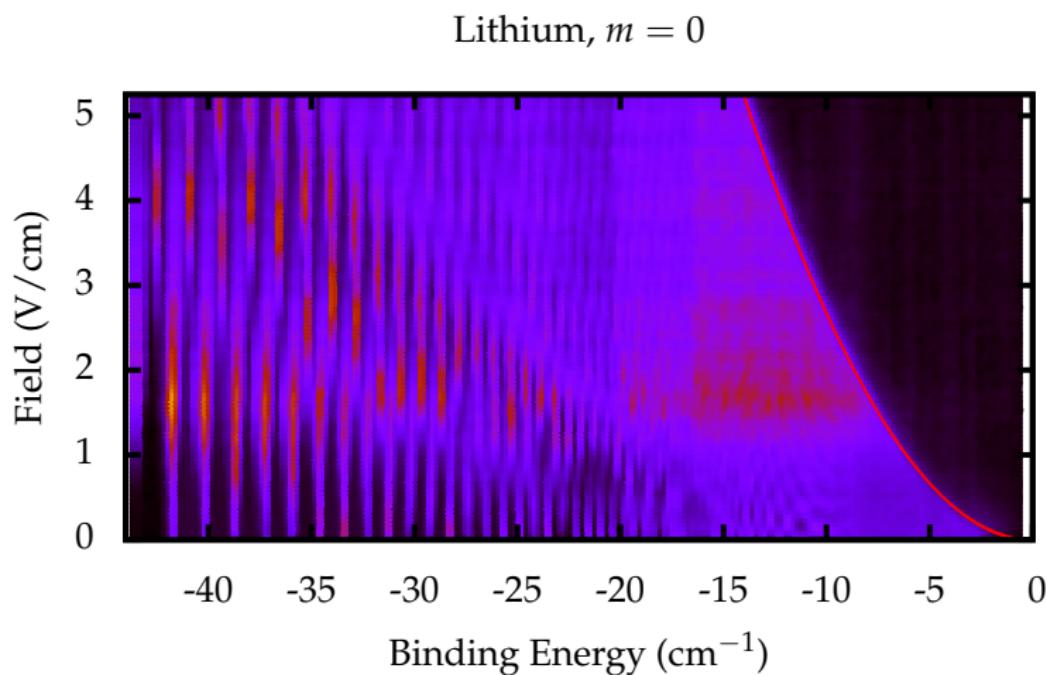
# Field Ionization



$$V(z) = \frac{-1}{|z|} - Ez$$

$$E = \frac{W^2}{4}$$

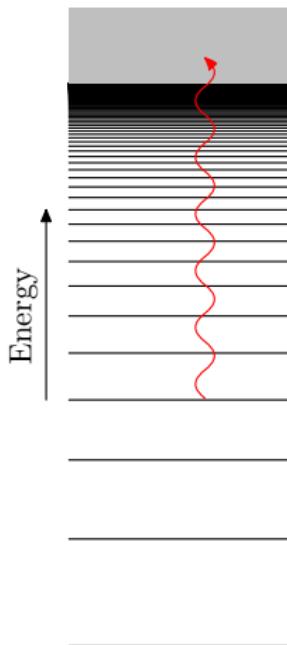
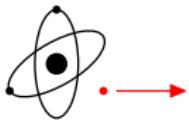
# Field Ionization



# Photoionization



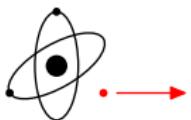
if  $\hbar\omega > W$ ,



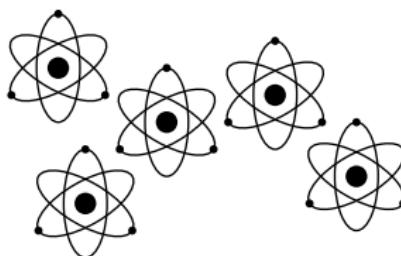
# Photoionization



if  $\hbar\omega > W$ ,

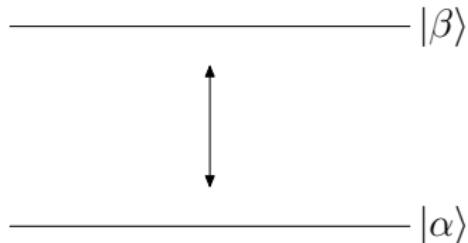


If we have some collection of atoms,



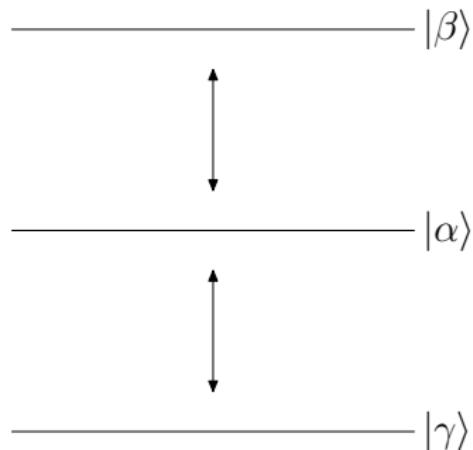
how do we calculate the ionization rate?

# Fermi's Golden Rule



**Fermi's Golden Rule:**  
 $\Gamma_1 = 2\pi|\langle\alpha|\mu E|\beta\rangle|^2\rho_f$

# Fermi's Golden Rule

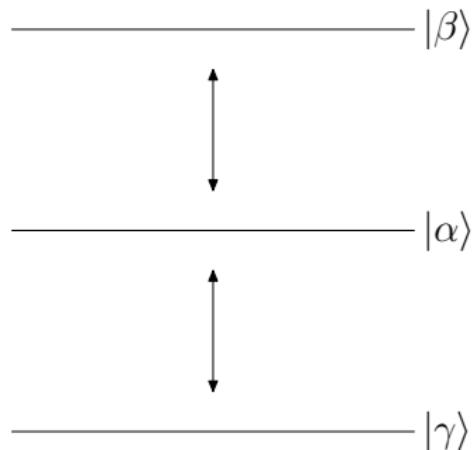


Fermi's Golden Rule:

$$\Gamma_1 = 2\pi |\langle \alpha | \mu E | \beta \rangle|^2 \rho_f$$

$$\Gamma_2 = 2\pi \left| \frac{\langle \gamma | \mu E | \alpha \rangle \langle \alpha | \mu E | \beta \rangle}{\Delta W} \right|^2$$

# Fermi's Golden Rule



Fermi's Golden Rule:

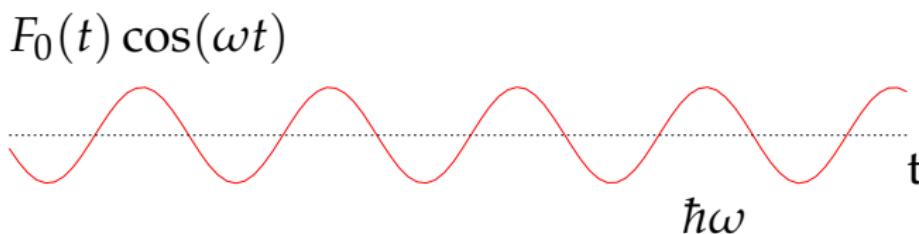
$$\Gamma_1 = 2\pi |\langle \alpha | \mu E | \beta \rangle|^2 \rho_f$$

$$\Gamma_2 = 2\pi \left| \frac{\langle \gamma | \mu E | \alpha \rangle \langle \alpha | \mu E | \beta \rangle}{\Delta W} \right|^2$$

$$\Gamma_N \propto E^{2N}$$

# What about microwaves?

If microwaves are just oscillating electric fields...



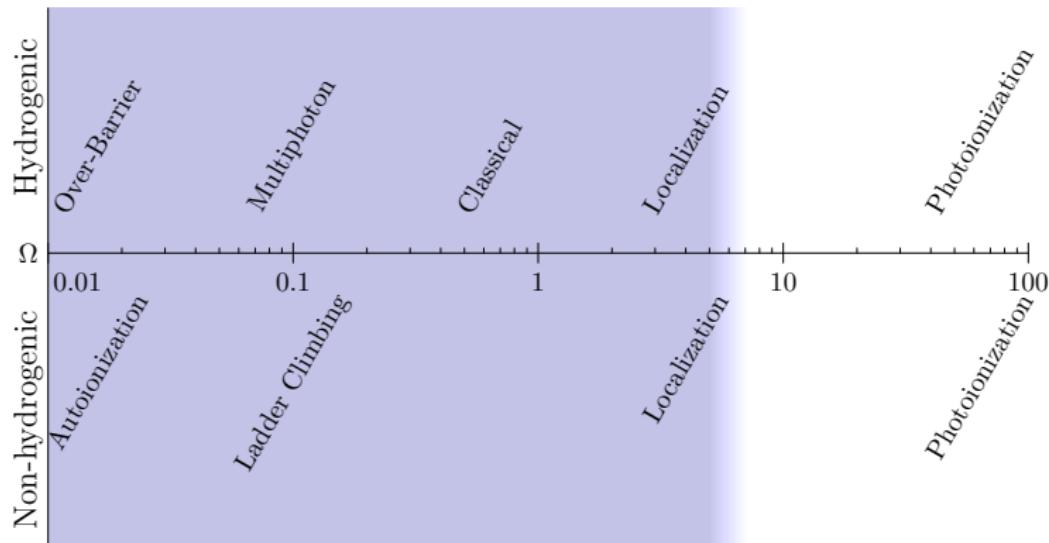
and if microwaves are just photons...

Can we connect field ionization to photoionization using microwave ionization of Rydberg atoms?

# Microwave Ionization

$$\Omega = \frac{\omega}{\omega_{Kepler}} = \omega n^3$$

$$E_0 = \frac{E}{E_{Coulomb}} = E n^4$$



What happens as we approach the photoionization limit?

# Outline

## Rydberg Atoms and How They Ionize

- Introduction to Rydberg Atoms

- Field Ionization

- Photoionization

- MW Ionization

## Experimental Setup

- Experimental Apparatus

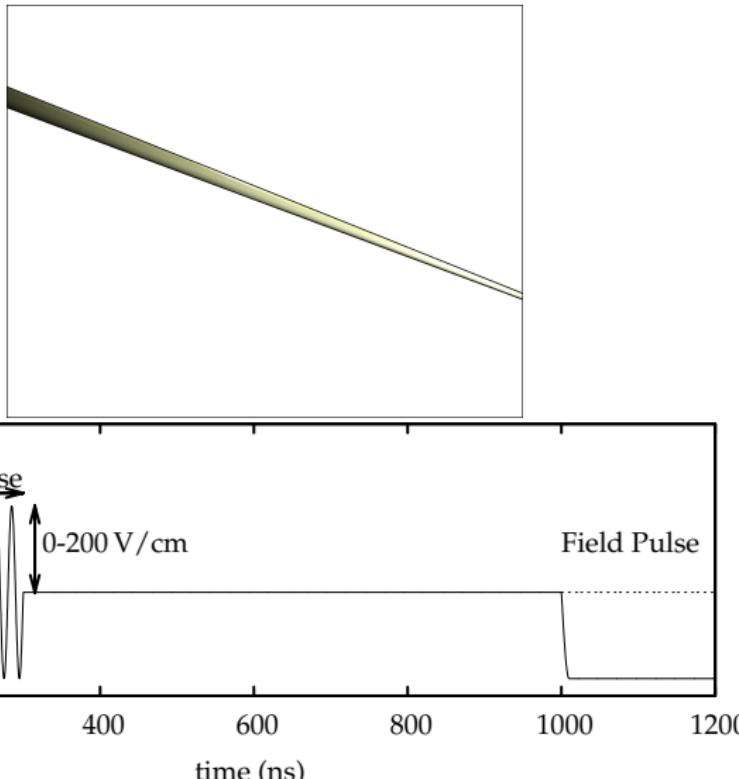
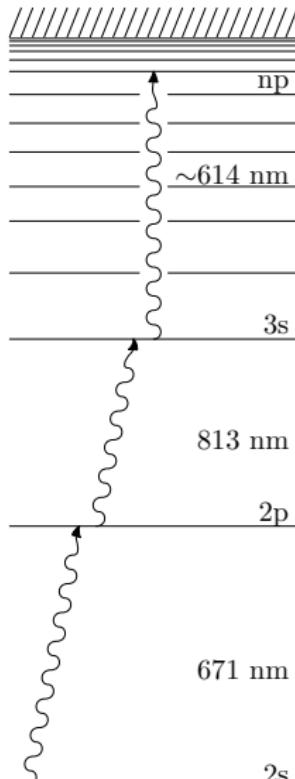
## Experimental Results

- Multiphoton MW Ionization

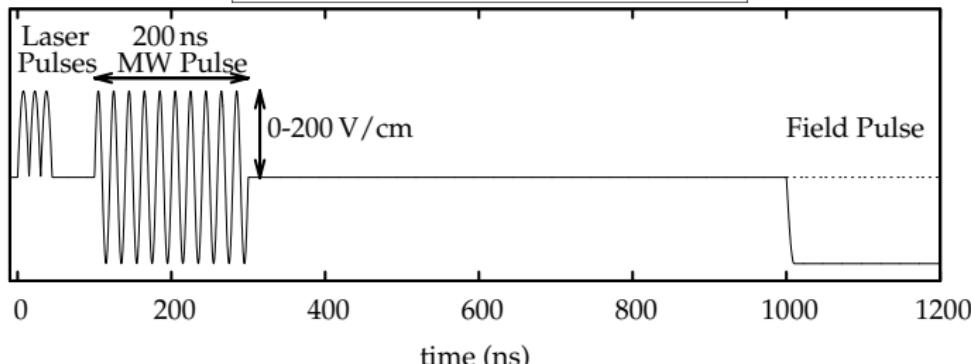
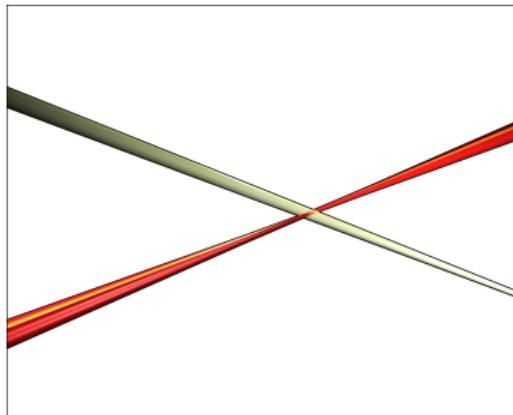
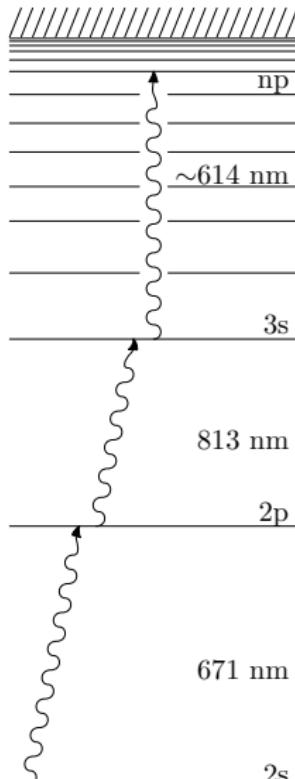
- Single Photon Ionization Rates

- Above-Threshold Bound States

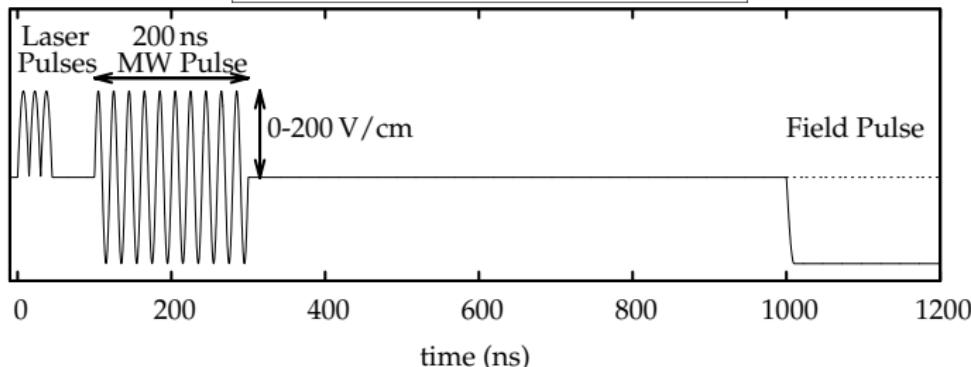
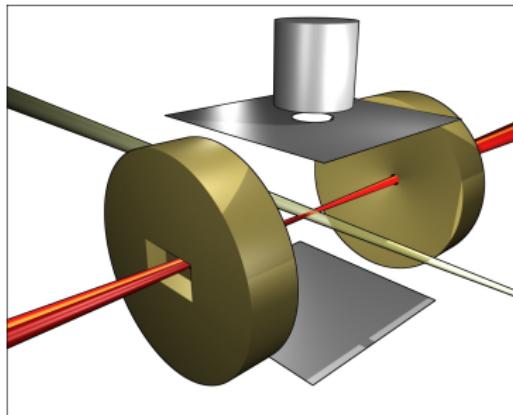
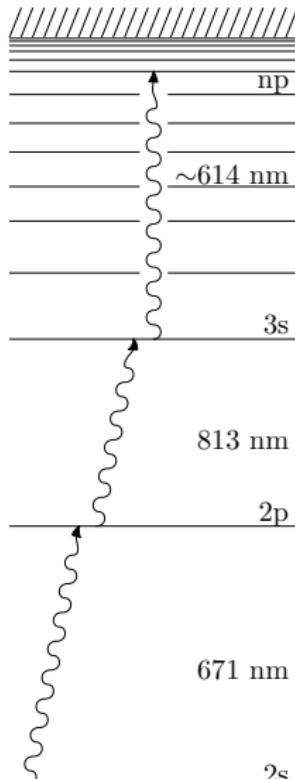
# Experimental Setup



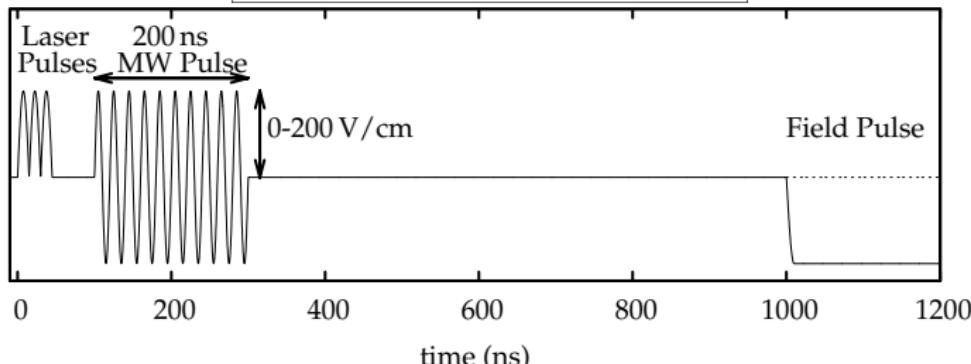
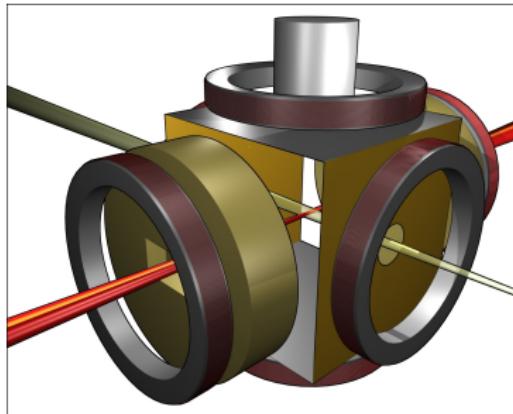
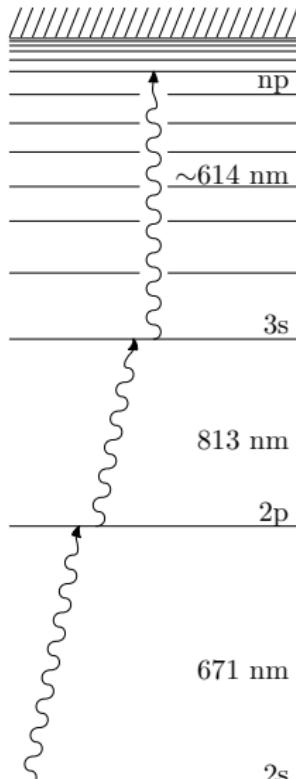
# Experimental Setup



# Experimental Setup



# Experimental Setup



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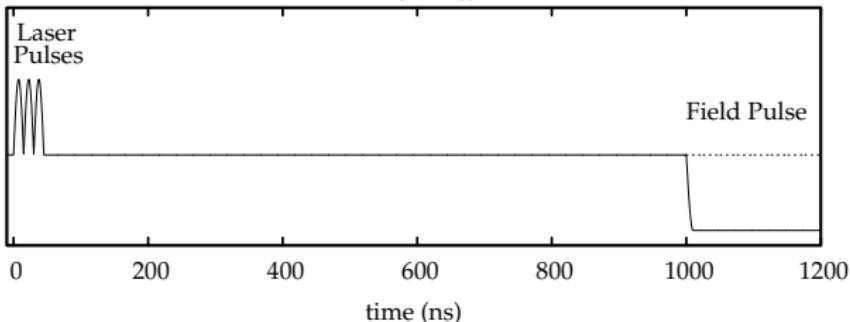
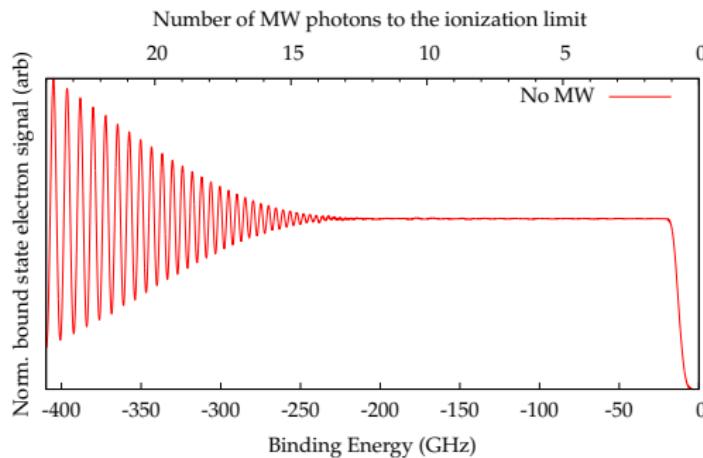
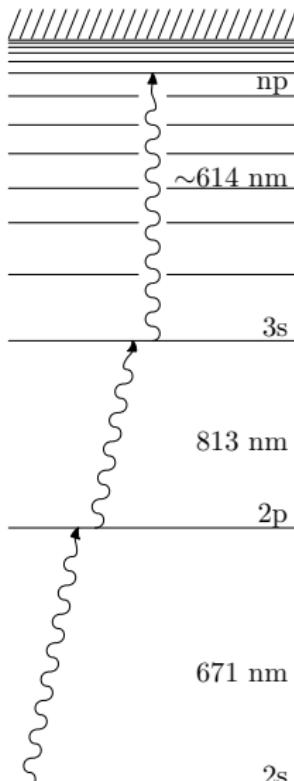
## Experimental Results

**Multiphoton MW Ionization**

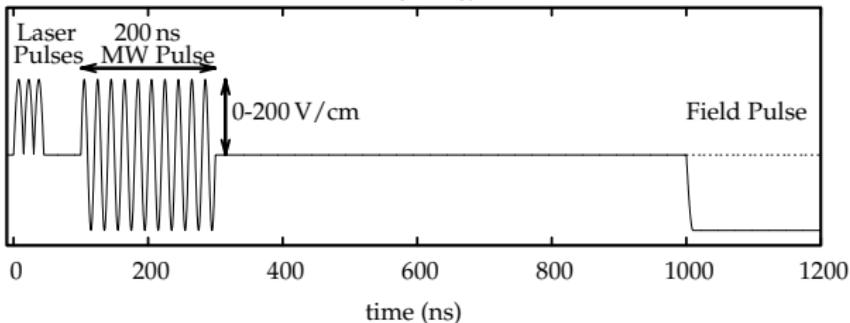
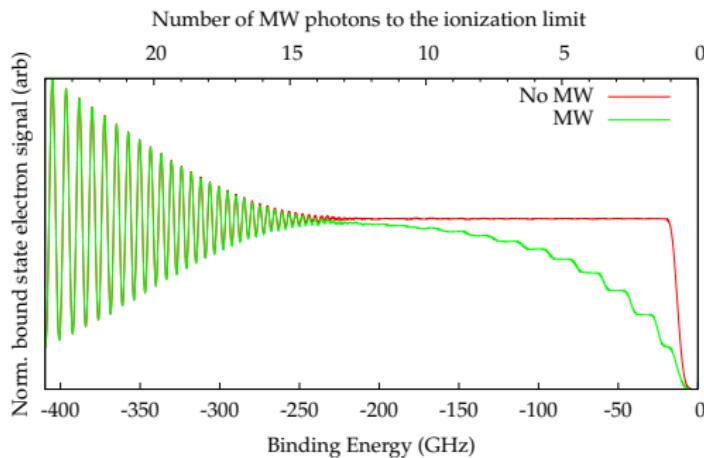
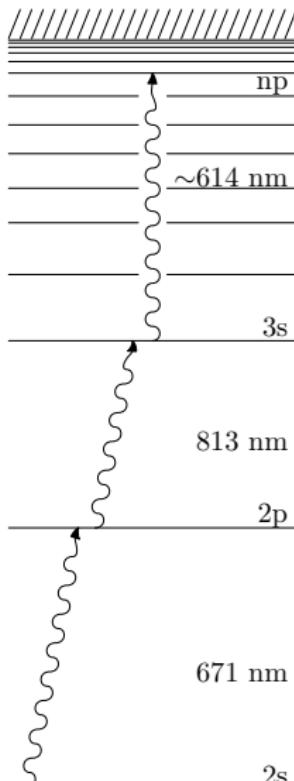
Single Photon Ionization Rates

Above-Threshold Bound States

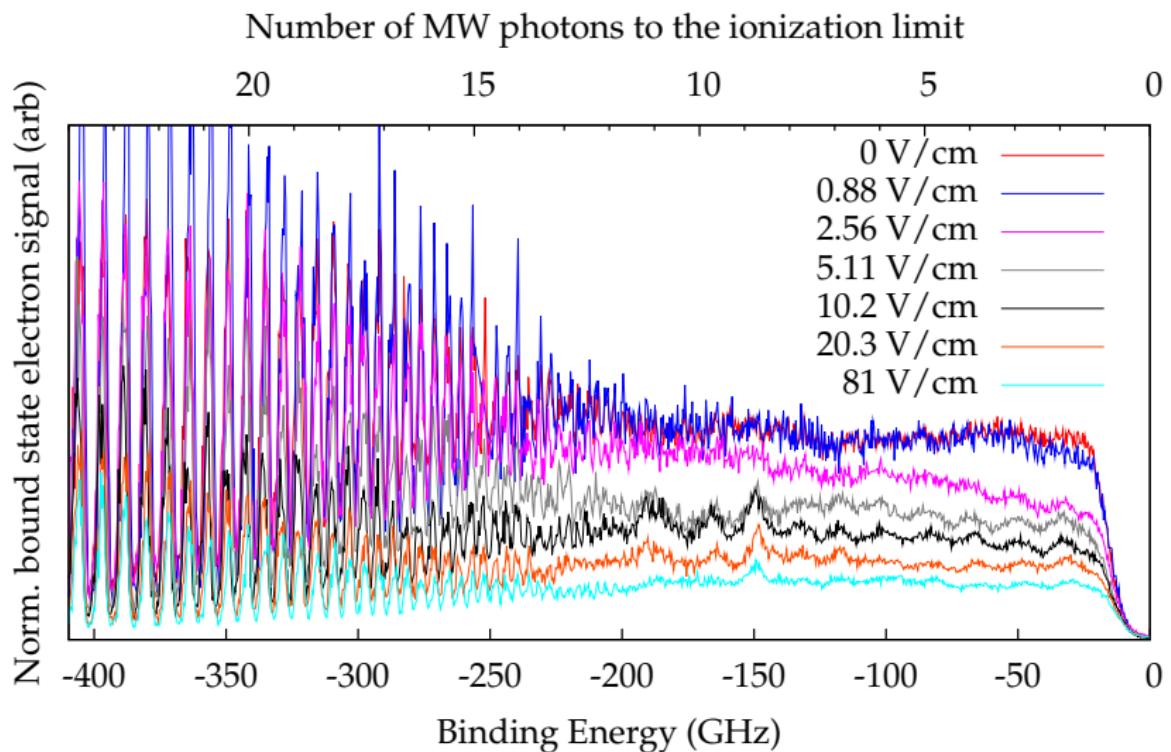
# Expected Results



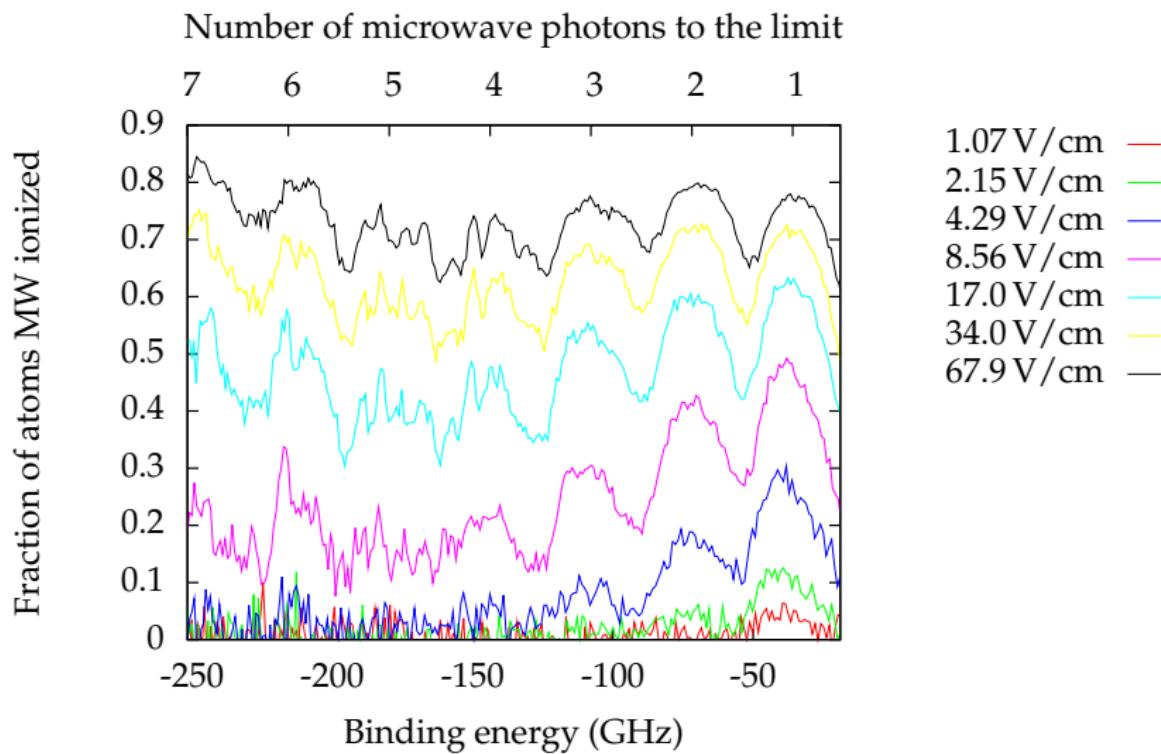
# Expected Results



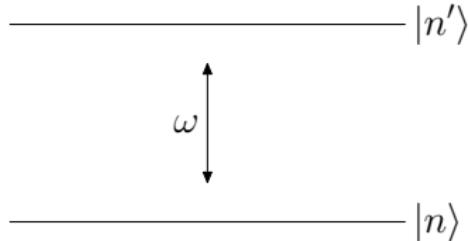
# Microwave Ionization Steps - 17 GHz



# Microwave Ionization Steps - 36 GHz



# Jensen *et al.* Model



$$\text{Rabi width} = \mu \cdot E = \frac{0.4108E}{\omega^{5/3} n^3}$$

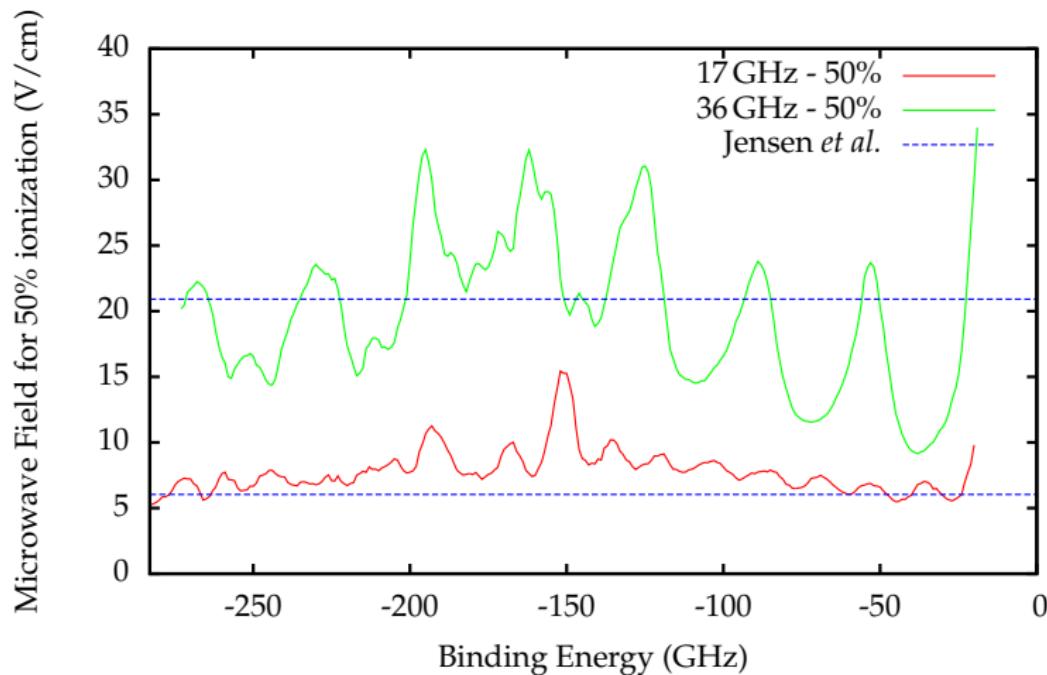
$$\text{State spacing} = \frac{1}{n^3}$$

MW ionization occurs when the Rabi width  $\geq$  state spacing

$$E = 2.4\omega^{5/3}$$

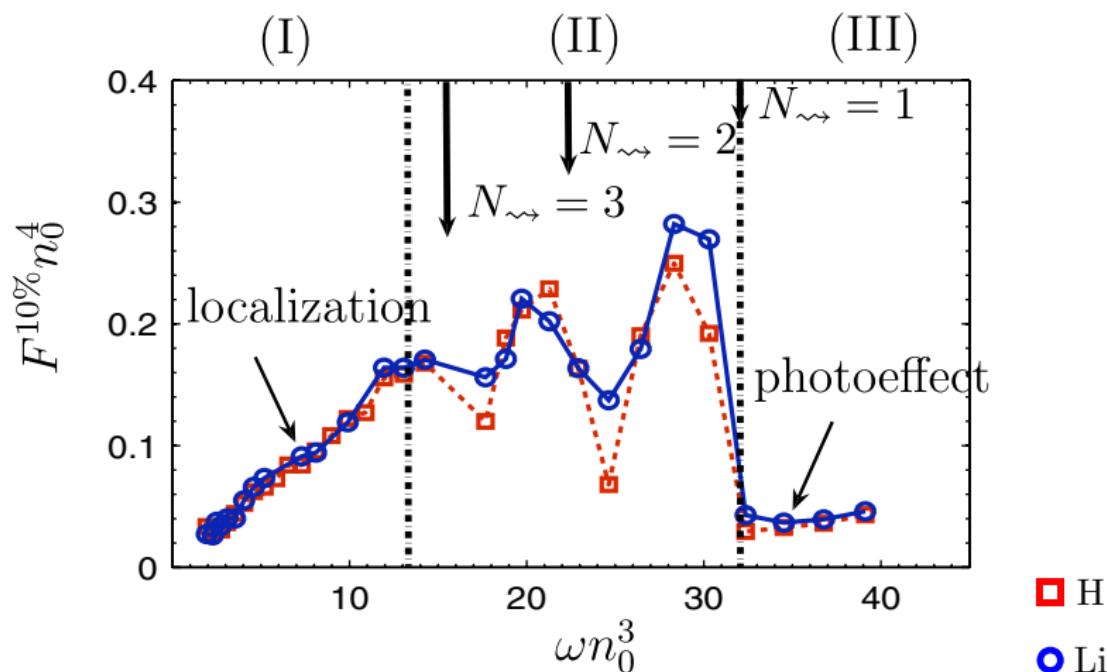
Jensen *et al.*, *Phys. Rev. Lett.* 62, (1989).

# Jensen *et al.* Comparison



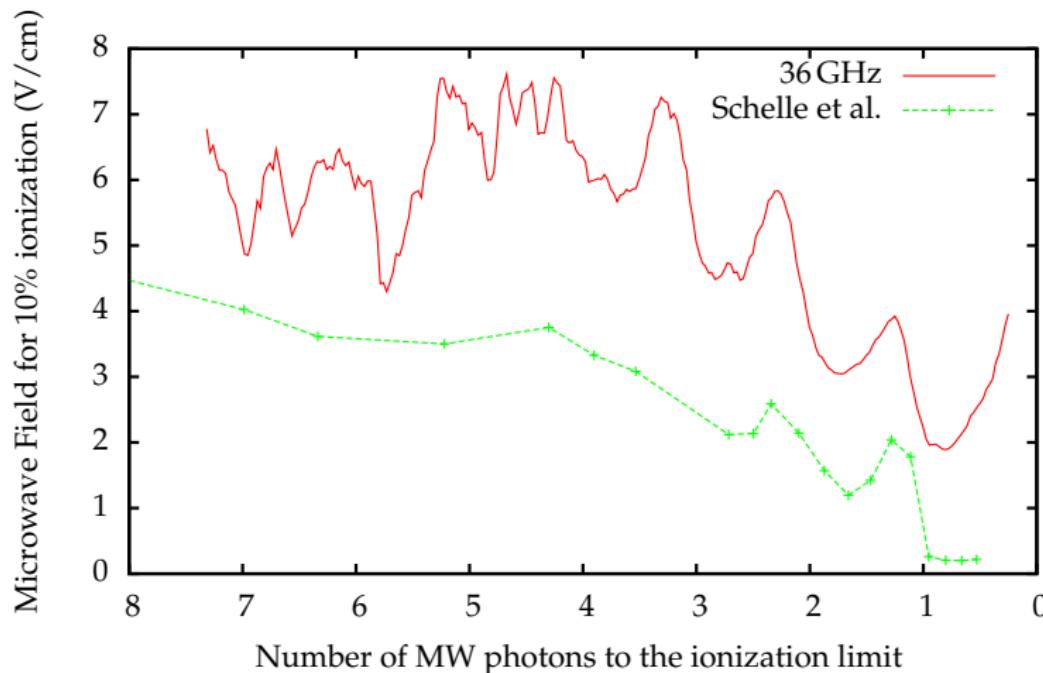
Jensen *et al.*, Phys. Rev. Lett. 62, (1989).

# Schelle *et al.* Comparison



Schelle *et al.*, Phys. Rev. Lett. 102, (2009).

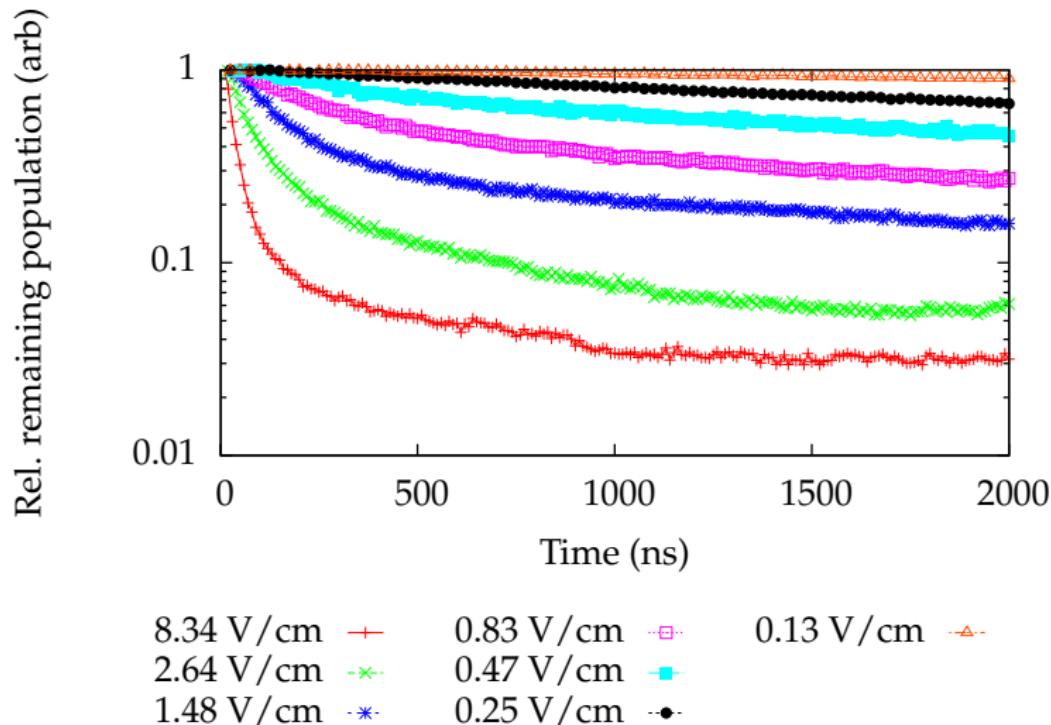
# Schelle *et al.* Comparison



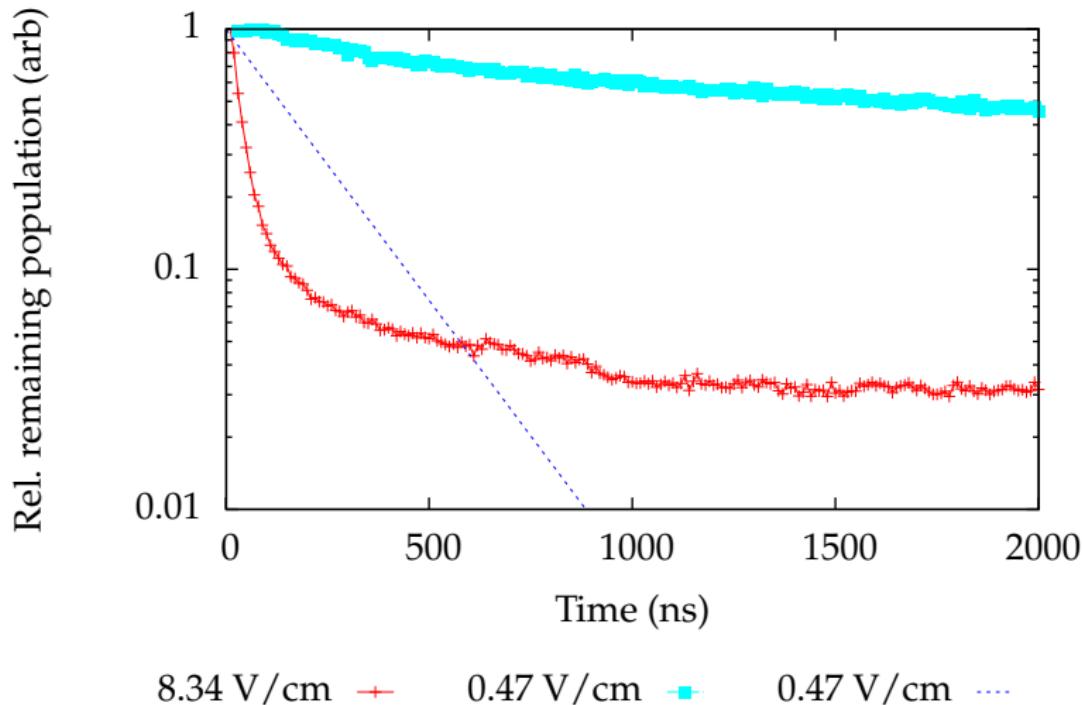
Schelle *et al.*, Phys. Rev. Lett. 102, (2009).

# Photoionization - Timing

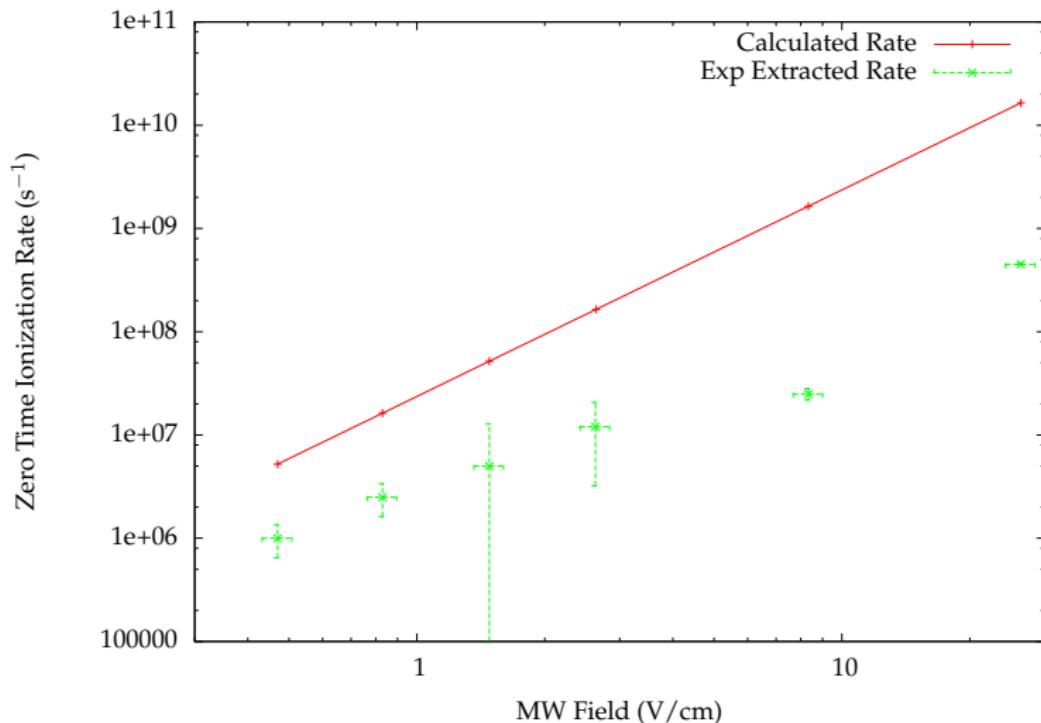
# Single Photon Ionization



# Single Photon Ionization



# Fermi's Golden Rule Comparison



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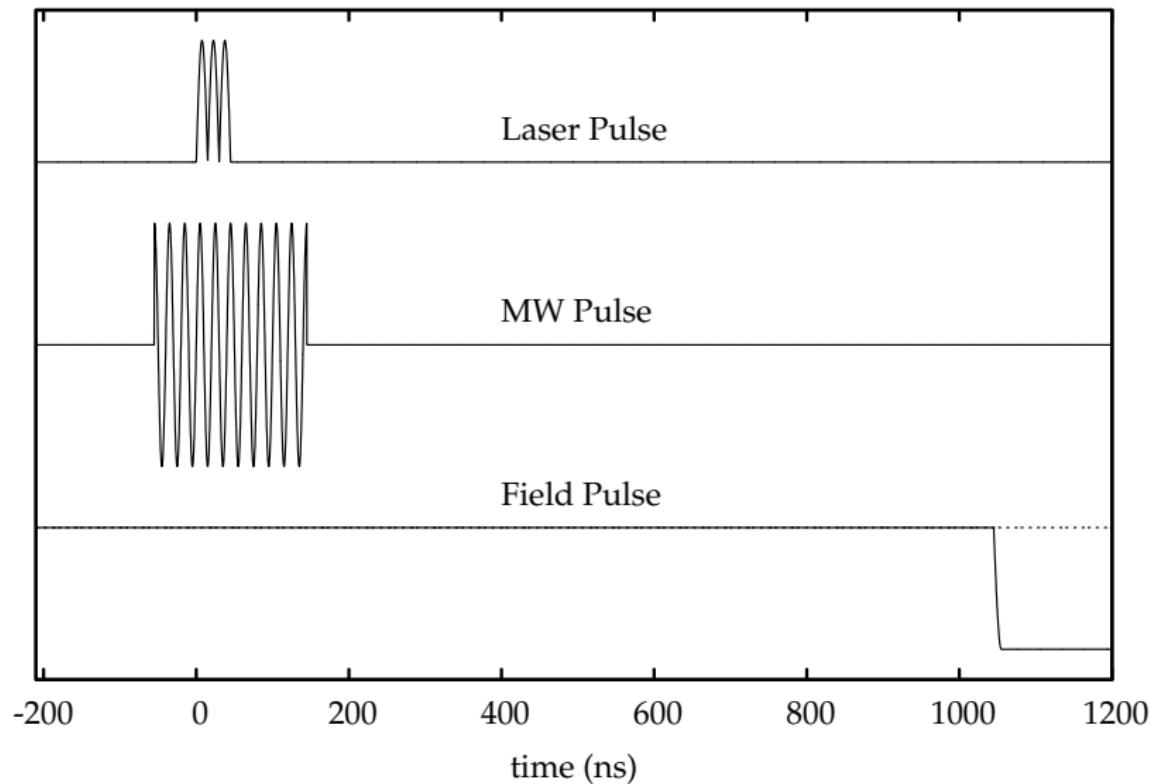
## Experimental Results

Multiphoton MW Ionization

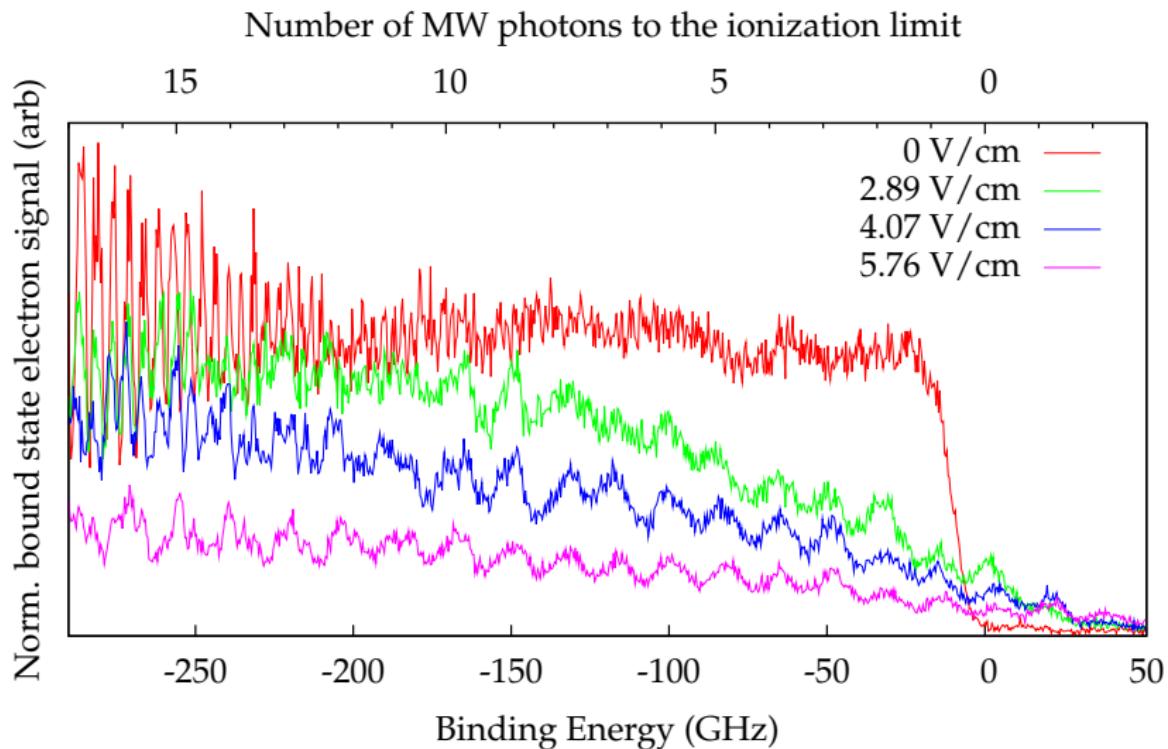
Single Photon Ionization Rates

Above-Threshold Bound States

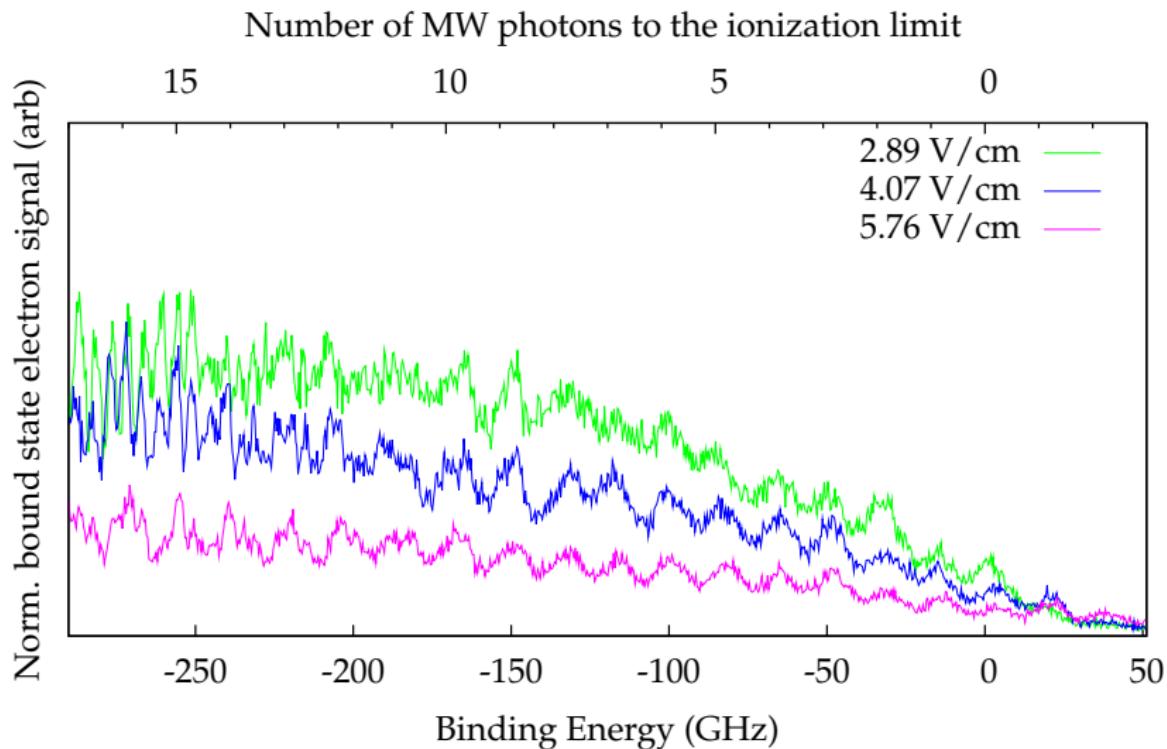
# Above-Threshold Bound States - Timing



# Above-Threshold Bound States

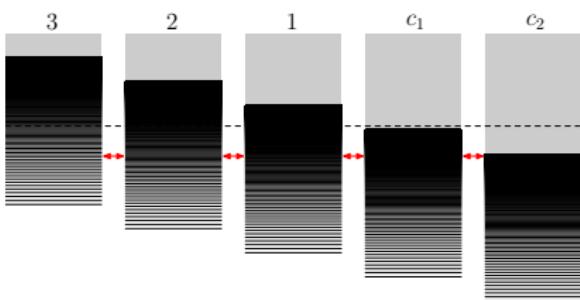


# Above-Threshold Bound States

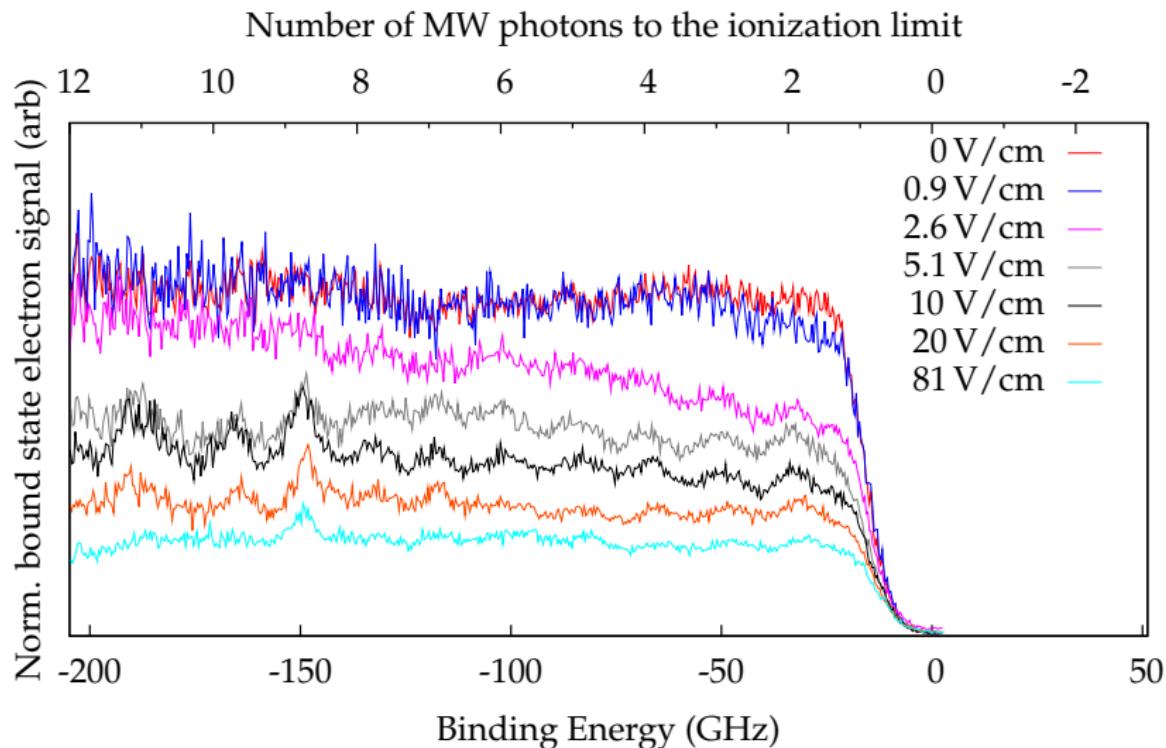


# MQDT-Floquet Model

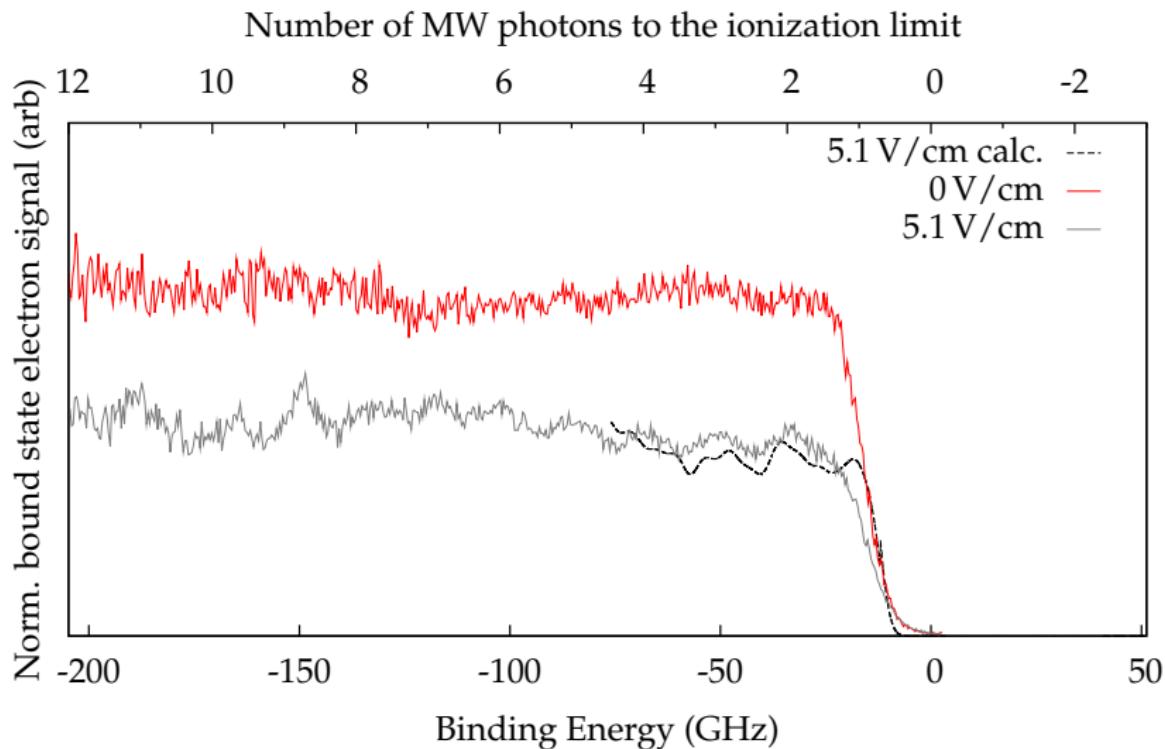
- ▶ Coherent coupling of states above and below ionization limit suggests a Multichannel Quantum Defect Theory - Floquet Model
- ▶ Floquet Theorem - Periodic perturbations yield periodic solutions



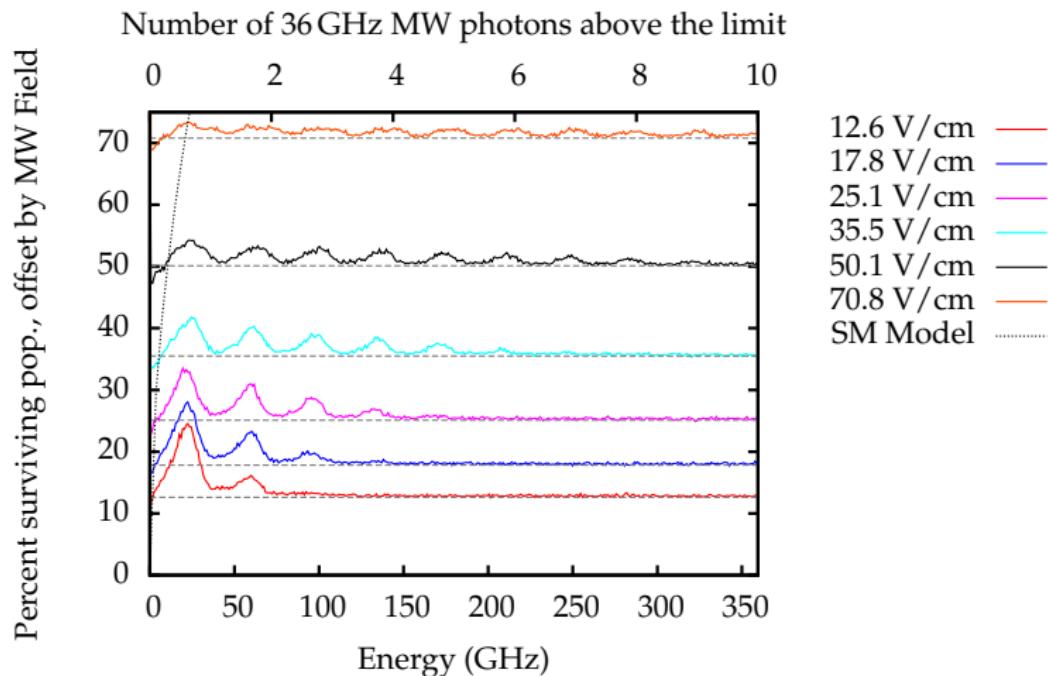
# Model Comparison



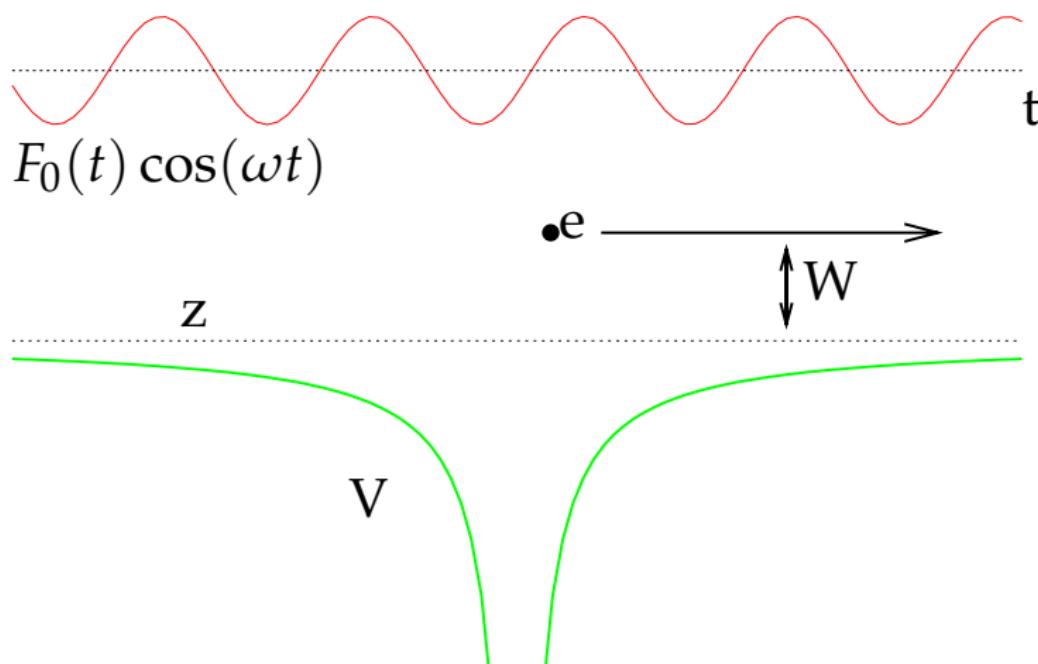
# Model Comparison



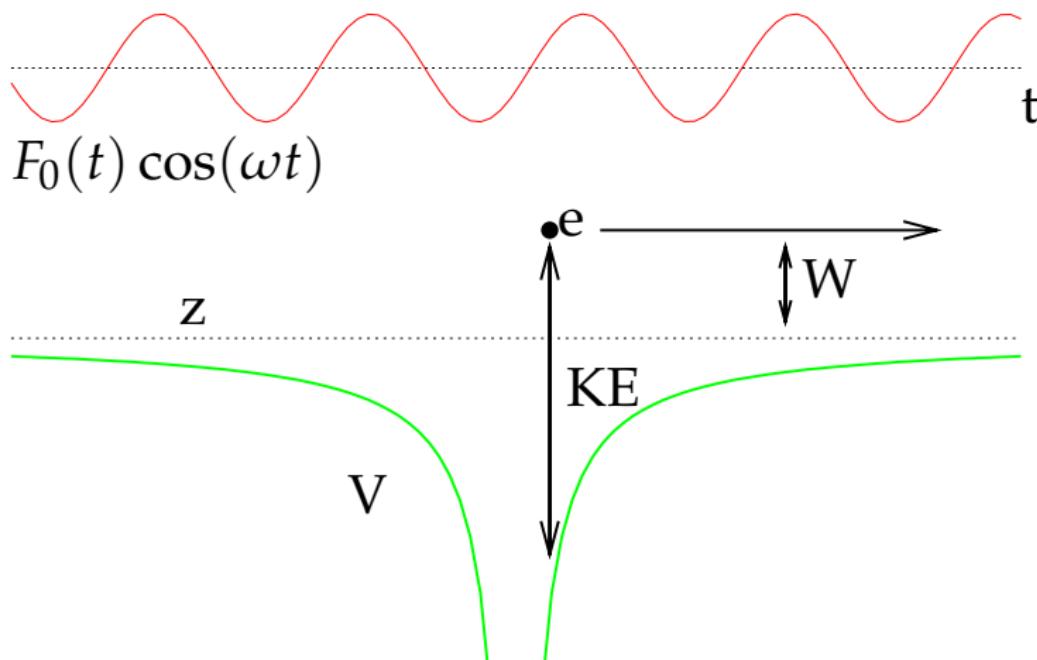
# Above-Threshold Bound States



# Simpleman's Model

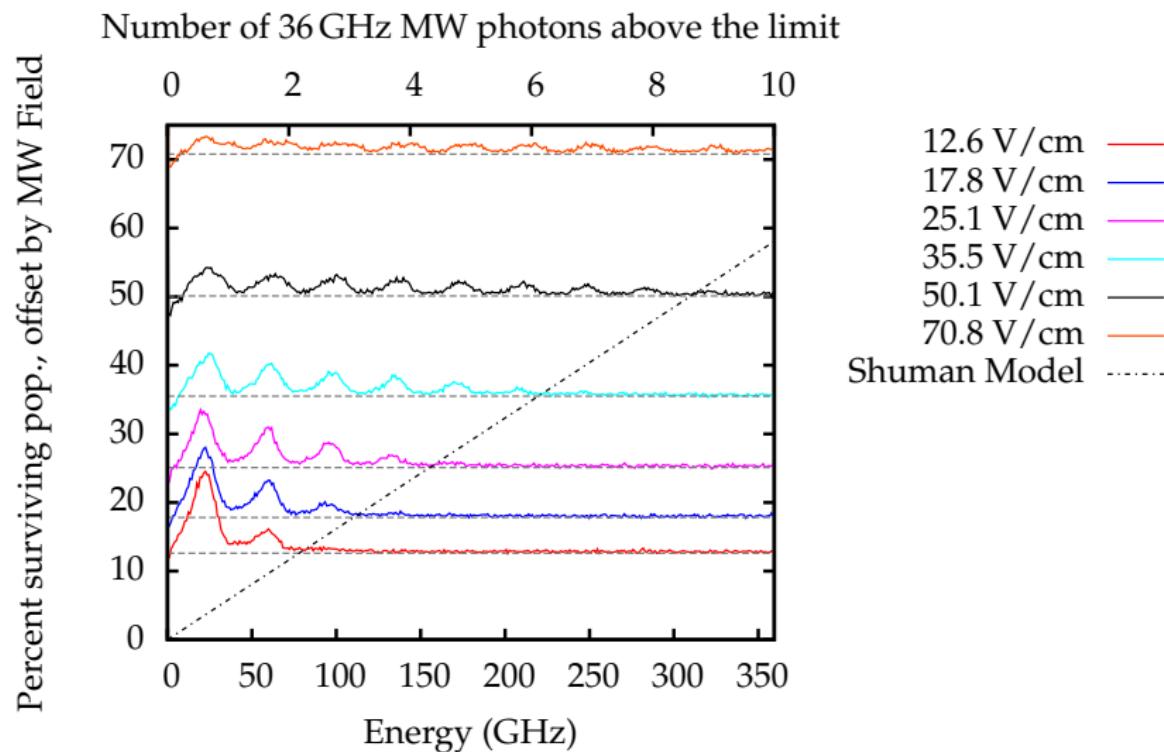


# New Classical Model



Shuman et al., *Phys. Rev. Lett.* 101, (2009).

# Above-Threshold Bound States



# Conclusions

- ▶ An Anderson Localization model crossing over to Fermi's Golden Rule does not match experimental results
- ▶ The coherent coupling of levels both above and below the ionization limit describes high scaled frequency microwave ionization
- ▶ A simple classical model illustrates population transfer from above the limit to bound states